Super strong nuclear force caused by migrating \bar{K} mesons - Revival of the Heitler-London-Heisenberg scheme in kaonic nuclear clusters

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Abstract: We have studied the structure of K^-pp comprehensively by solving this threebody system in a variational method, starting from the Ansatz that the Λ (1405) resonance ($\equiv \Lambda^*$) is a K^-p bound state. The structure of K^-pp reveals a molecular feature, namely, the K^- in Λ^* as an "atomic center" plays a key role in producing strong covalent bonding with the other proton. We point out that strongly bound \bar{K} nuclear systems are formed by "super strong" nuclear force due to migrating real bosonic particles \bar{K} a la Heitler-London-Heisenberg, whereas the normal nuclear force is caused by mediating virtual mesons. We have shown that the elementary process, $p + p \rightarrow K^+ + \Lambda^* + p$, which occurs in a short impact parameter and with a large momentum transfer, leads to unusually large self-trapping of Λ^* by the involved proton, since the Λ^* -p system exists as a compact doorway state propagating to K^-pp .

Keywords: K meson, nuclear force, molecule, Heitler-London, few-body problems

1. Introduction

In 1932, right after the discovery of the neutron, Heisenberg¹ tried to explain the nuclear force (for instance, the proton-neutron interaction) with the idea of "Platzwechsel" of a migrating particle, which had been known as the mechanism for the covalency in the hydrogen molecule, first clarified by Heitler and London in 1927.²) This "molecule-type bonding" mechanism can be written as

Heitler-London-Heisenberg:
$$e^-p + p \leftrightarrow p + e^-p$$
.
[1.1]

Since this " e^-p " cannot be identified with the neutron for obvious reasons, this idea was unsuccessful, and was abandoned. Instead of a "migrating real" particle, Yukawa³ introduced a "mediating virtual" boson for explaining the nuclear force as

Nuclear force by Yukawa: $p \leftrightarrow \pi^+ + n$, $n \leftrightarrow \pi^- + p$. [1.2] This hypothetical particle was eventually discovered, and Yukawa's idea of a mediating virtual particle was established as the fundamental concept for understanding all the forces including the electroweak interaction. In the present paper we point out that the \bar{K} meson, as a "real migrating" particle, plays a unique role in producing strong bonding of nucleons as

Super strong nuclear force:
$$K^-p + p \leftrightarrow p + K^-p$$
.
[1.3]

One can say that this is the revival of the forgotten Heitler-London-Heisenberg scheme for nuclear binding force. In the following sections we describe briefly how this view has come out from our theoretical studies of an exotic bound system K^-pp . We also foresee perspectives of this view toward kaon condensation. Preliminary reports of the present results are documented,⁴⁾ and their full accounts will be published elsewhere.⁵⁾

2. Kaonic nuclear bound states

Recently, exotic light nuclear systems involving a \bar{K} (K^- and \bar{K}^0) meson as a constituent have been predicted based on phenomenologically constructed $\bar{K}N$ interactions.⁶⁾⁻¹¹ The basic ingredient for this new family of nuclear states, often called *kaonic nuclear clusters*, is the strongly attractive $I = 0 \ \bar{K}N$

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interaction, which accommodates the K^-p bound state, identified to the known Λ (1405) resonance in the $\Sigma\pi$ channel (hereafter, expressed as Λ^*) with a binding energy of $B_K = 27$ MeV and a width of Γ = 40 MeV.¹²) Since the Λ (1405) resonance is largely populated in the K^- absorption at rest in ⁴He ¹³) and also in nuclear emulsion,¹⁴) it is very likely to be the $I = 0 \ \bar{K}N$ bound state. The $\bar{K}N$ interaction was also derived theoretically (see, for instance, Refs. 15 and 16).

The most spectacular property of the predicted kaonic nuclei is in their extremely high densities; the average density, $\rho_{av} \sim 0.5 \text{ fm}^{-3}$, reaches about 3 times as much as the normal nuclear density $\rho_0 \sim 0.17 \text{ fm}^{-3}$. This is an enormous contrast to the normal nuclear systems, in which the nuclear density is always a constant. The \bar{K} produces extra binding of nucleons, which overcompensate the stiff nuclear incompressibility. In order to understand this feature we study the most fundamental unit, K^-pp .

The lightest system following the " Λ (1405) = K^-p Ansatz", K^-pp , was predicted to exist with $M = 2322 \text{ MeV}/c^2$, $B_K = 48 \text{ MeV}$ and $\Gamma = 61 \text{ MeV}$.⁷ Recently, Faddeev calculations have been carried out to obtain the pole corresponding to K^-pp by Shevchenko *et al.*¹⁷ and by Ikeda and Sato.¹⁸) Their results are consistent with ours.

3. Structure of K^-pp

In our study the ATMS variational method¹⁹⁾ was employed together with the bare $\bar{K}N$ interaction of AY⁶⁾ and the bare NN interaction of Tamagaki.²⁰⁾ The three-body variational wave function of $\bar{K}NN$ with a number definition $(1, 2, 3) = (\bar{K}, N, N)$ is given as

$$\Psi = [\Phi_{12} + \Phi_{13}] | T = 1/2 \rangle$$
 [3.1]

where

$$\Phi_{12} = [f^{I=0}(r_{12}) P_{12}^{I=0} + f^{I=1}(r_{12}) P_{12}^{I=1}] \\ \times f_{NN}(r_{23}) f(r_{31}), \qquad [3.2]$$

$$\Phi_{13} = f(r_{12}) f_{NN}(r_{23}) \\ \times [f^{I=0}(r_{31}) P_{31}^{I=0} + f^{I=1}(r_{31}) P_{31}^{I=1}], \qquad [3.3]$$

with $P_{12}^{I=0} = (1 - \tau_{\bar{K}} \cdot \tau_{\bar{N}})/4$ and $P_{12}^{I=1} = (3 + \tau_{\bar{K}} \cdot \tau_{\bar{N}})/4$. The functions $f^{I=0}(r_{ij})$ and $f^{I=1}(r_{ij})$ are scattering correlation functions of the particle pair (i, j) for the I = 0 and $I = 1 \bar{K}N$ interactions, respectively, and $f_{NN}(r_{23})$ is that for the NN pair,

and $f(r_{ij})$ is for the off-shell case. The T = 1/2 state consists of two isospin eigenstates as

$$|T = 1/2\rangle = \sqrt{\frac{3}{4}} \left[(\bar{K}_1 N_2)^{0,0} p_3 \right] + \sqrt{\frac{1}{4}} \left[-\sqrt{\frac{1}{3}} (\bar{K}_1 N_2)^{1,0} p_3 + \sqrt{\frac{2}{3}} (\bar{K}_1 N_2)^{1,1} n_3 \right],$$
[3.4]

where $(\bar{K}_1 N_2)^{I,I_z}$ is for the isospin (I, I_z) . Among these the first term corresponds to $\Lambda^* p$.

The predicted structure of K^-p and K^-pp is shown in Fig. 1. The "nucleus" pp does not exist, but the K^- can combine two protons into a strongly bound system, when they are in a spin-singlet state.

The effective potentials as functions of the relative distances of \bar{K} -(NN) and N- $(\bar{K}N)$ are extracted from the obtained total wave function, as shown in Fig. 1 (Left). The distributions of the relative distances and the momenta of the constituent particle pairs, namely, \bar{K} -N, \bar{K} -(NN), $(\bar{K}N)$ -N, and N-N, were calculated, as shown in the middle. For comparison the \bar{K} -N density distribution in free Λ^* is also shown. The N-N rms distance is 1.90 fm, which is significantly smaller than the average inter-nucleon distance in normal nuclei (2.2 fm²¹), and is much smaller than the rms distance of p-n in d (3.90 fm). The rms radius of \bar{K} with respect to (NN) is 1.35 fm, close to the rms distance of \bar{K} -N in Λ (1405), 1.36 fm.

We compare in Fig. 1 (Right) the \bar{K} -N distance distribution of the $\bar{K}N$ pair in K^-pp , $\rho_{\bar{K}-N}(K^-pp)$, with that in $\Lambda(1405)$, $\rho_{\bar{K}-N}(\Lambda^*)$. The former $(R_{\bar{K}-N}^{\rm rms} = 1.57 \text{ fm})$ is significantly broader than the latter (1.36 fm). We decompose the density distribution into the $\bar{K}N^{I=0}$ and $\bar{K}N^{I=1}$ parts, as The I = 0-pair distribution has a shape shown. closer to $\rho_{\bar{K}-N}(\Lambda^*)$, whereas the I=1 part is widely distributed due to the smaller attractive interaction. When $K^{-}(1)$ resides with Proton (2) with a probability of 0.5, the I=0 component of the wave function Φ_{12} in (3.2) dynamically increases to 1 due to the strong $\bar{K}N^{I=0}$ interaction. Adding an intensity $(0.5 \times 1/4 = 0.125)$ from Proton (3), we expect the total intensity to be $0.625 \rho_{\bar{K}-N}(\Lambda^*)$, which accounts for the calculated $\rho_{\bar{K}-N}(K^-pp)$ very well. This means that $K^{-}(1)$ in $K^{-}pp$ resides partially around Proton (2) in a form of Λ (1405), and partially around Proton (3), as given by the total wave function. This indicates that the structure of

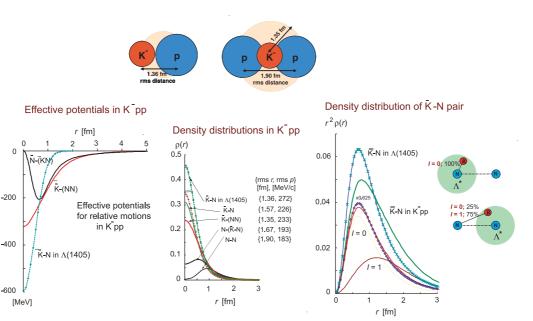


Fig. 1. (Upper) Schematic structure of K^-p and K^-pp . (Lower Left) The effective potentials for relative motions of N- $(\bar{K}N)$ and \bar{K} -(NN), deduced from the exact variational wavefunction for K^-pp . The \bar{K} -N potential in Λ (1405) is also shown. (Lower Middle) Density distributions of various coordinates in K^-pp as well as Λ (1405) = K^-p . (Lower Right) Comparison of the density distributions, $r^2\rho(r_{KN})$, of the \bar{K} -N distance in the $\bar{K}N$ pair in Λ (1405) and in K^-pp . The latter is decomposed into the I = 0 and I = 1 pairs. The density distribution in Λ (1405) after multiplication of a factor 0.625 is also shown.

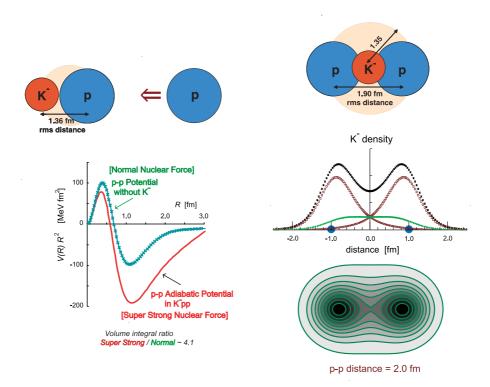


Fig. 2. (Left) The adiabatic potential $(V(R)R^2)$, when a proton approaches a bound K^-p "atom" (Λ^*) , as a function of the distance between p and p. The Tamagaki potential for the normal V_{NN} interaction is shown for comparison. (Right) The molecular structure of K^-pp . The projected density distributions of K^- in K^-pp with a fixed p-p distance (= 2.0 fm) and the corresponding K^- contour distribution are shown.

 Λ (1405) is nearly unchanged when it dissolves into this "nucleus". In other words, the Λ (1405) state, though modified, persists in a nuclear system. This aspect justifies the Λ (1405) doorway model.⁷⁾

4. Molecular aspect of K^-pp and super strong nuclear force

The present kaonic nuclear cluster K^-pp can be interpreted as a kaonic hydrogen molecular ion in the sense that K^- migrates between the two protons, producing "strong covalency" through the strongly attractive $\bar{K}N^{I=0}$ interaction. This is essentially the mechanism of Heitler and London² for the hydrogen molecule, though the nature of the interaction is totally different and the migrating particle is much heavier and bosonic. Figure 2 (Left) shows the adiabatic potential ($V(R) R^2$), when a proton approaches a Λ (1405) particle, as a function of the *p*-*p* distance. The deep potential indicates that a proton approaching an isolated Λ^* from a large distance becomes quickly trapped and dissolved into the bound state of K^-pp .

Figure 2 (Right) shows the projected distribution of K^- along the *p*-*p* axis and the contour distribution of K^- , in the case that the *p*-*p* distance is fixed to 2.0 fm (this case resembles the ground state of K^-pp , as the calculated rms distance is 1.9 fm). The K^- is distributed, not around the center of *p*-*p*, but around each of the two protons. The K^- distribution is composed of the "atomic" part, as shown by brown dotted curves, and the exchange part (green broken curve) *a la* Heitler and London.

We emphasize that the strong $I = 0 \ \bar{K} N$ attraction produces a large exchange integral,

$$\sum_{\{i,j\}=\{2,3\},\{3,2\}} \langle \Phi_{1i} | v_{\bar{K}N}(12) + v_{\bar{K}N}(13) | \Phi_{1j} \rangle$$

= -52.6 MeV, [4.1]

which is the source for the deeper binding of K^-pp as compared with K^-p . Despite the drastic dynamical change of the system caused by the strong $\bar{K}N$ interaction the identity of the "constituent atom", Λ^* , is nearly preserved because of the presence of a short-range repulsion between the two protons. The molecule K^-pp resembles a tightly bound Λ^*-p , which we call Λ^*p doorway in the formation process.

Thus, we have demonstrated that the strong $\bar{K}N$ attraction produces a very strong molecular type bonding of the two protons. This adiabatic potential (red curve) as shown in Fig. 2 (Left) can be

called Super Strong Nuclear Force, as compared with the ordinary nuclear force (green curve). Not only the depth of the potential, but also the long range attractive part due to the covalent nature and the relatively smaller short-range repulsive part produce an enormous binding in \bar{K} -migrating nuclear systems, as shown in Fig. 2 (Left). The "super strong" / "normal" ratio of the volume integrated strength is 4.1.

5. Dominance of $\Lambda^* p$ doorway in $K^- pp$ production in NN collisions

We expect that the K^-pp state as a Λ^*p composite can be formed in the p + p reaction:

$$p + p \to K^+ + (\Lambda^* p) \to K^+ + K^- pp.$$
 [5.1]

The reaction diagram is shown in Fig. 3 (Left). Essentially, the spectral function for K^-pp is composed of the following three factors: i) the collision range $1/m_B$, taken to be the ρ meson mass; $m_B = m_{\rho} = 770 \text{ MeV}/c^2$, ii) the momentum transfer, $Q \sim 1.6 \text{ GeV}/c$, and iii) the structure function, depending on the rms distance $R(\Lambda^*p)$ of the Λ^* -p system.

The calculated spectral function at $T_p = 4 \text{ GeV}$ at forward angle in the scale of $E(\Lambda^* p) = 27 \text{ MeV} B_K$ is presented in Fig. 3 (Right). Surprisingly, in great contrast to ordinary reactions, the spectral function is peaked at the bound state with only a small quasi-free component. This means that the sticking of Λ^* and p is extraordinarily large. This dominance of $\Lambda^* p$ sticking in such a large-Q reaction can be understood as originating from the matching of the small impact parameter with the small size of the bound state. It is vitally important to examine our results experimentally. An experimental observation of K^-pp in pp collision may be revealed in a past experiment DISTO at Saclay²²⁾ as well as in a planned experiment at GSI.²³⁾ If a bound-state peak is found, it will not only confirm the existence of K^-pp , but also prove the compactness of the \bar{K} cluster.

6. Why does \bar{K} produce shrunk nuclear systems?

The constancy of nuclear density, $\rho \sim \rho_0 \sim 0.17$ fm⁻³, which is believed to be almost the nuclear physics "law", results from the balance between the short-range nuclear repulsion and the long-range attraction of the ordinary nuclear force. In normal nuclei the average inter-nucleon distance is

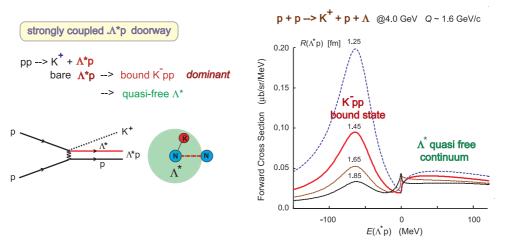


Fig. 3. (Left) Diagram for the $p(p, K^+)K^-pp$ reaction. (Right) Calculated spectral shape for different rms distances $R(\Lambda^*p)$, arbitrarily chosen. The binding energy of K^-pp is set to be 86 MeV for the $\bar{K}N$ interaction which is 17 % enhanced. In this case, $R(\Lambda^*p) = 1.45$ fm is realistic.

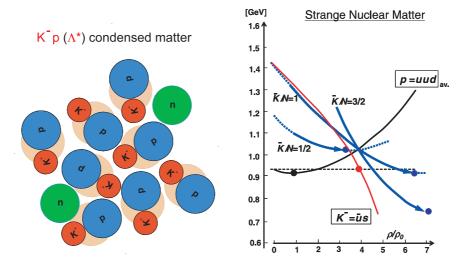


Fig. 4. (Left) Speculated $K^- p = \Lambda^*$ matter with a quasi- Λ^* as an "atomic" constituent, where K^- 's migrate among protons, producing high-density strange matter. (Right) Speculated diagrams for the density dependences of the bound-state energies of various baryon composite systems $(pK^-)^m n^n$. The $\bar{K}N$ energy is represented by the red curve, and the nuclear compression by the black curve. The total energies for representative fractions of K^-/N (=1/2, 1 and 3/2) are depicted by respective blue curves, showing minima at high density and low energy. Density-dependent enhanced $\bar{K}N$ interactions with relativistic correction are assumed.

$$d_{NN} \sim 2 \sqrt[3]{\frac{3}{4\pi\rho_0}} \sim 2.2 \text{ fm},$$
 [6.1]

 $f_c = \rho_N / \rho_0 \sim 2.3$. This situation seems to be almost unchanged by the normal nuclear force.

when we adopt Bethe's estimate based on a closepacked sphere approximation.²¹⁾ The nucleon rms radius, $r_{\rm rms} \sim 0.86$ fm, corresponds to a nucleon volume of $v_N \sim 2.66$ fm³ and to a nucleon density of $\rho_N \sim 0.38$ fm⁻³. This means that nucleons occupy the nuclear space with a compaction factor of The hard core part of the *N*-*N* interaction plays an essential role in keeping the nuclear density constant. In an intuitive picture it is related to the Pauli blocking in the *u*-*d* quark sector. This situation is common for all hadron-hadron interactions except for the case of \bar{K} , which, composed of $s\bar{u}$ (K^-) or $s\bar{d}$ (\bar{K}^0), includes no (u, d) quark. Thus, the KN interaction is expected to be dominated by the u- \bar{u} and d- \bar{d} attraction without short-range repulsion. From this consideration we understand intuitively why normal nuclei are difficult to compress and why only the \bar{K} meson produces dense nuclear systems. The intruding \bar{K} meson, as a "messenger of \bar{u}/\bar{d} quark", is expected not only to cause super strong nuclear force by its strong covalency, but also to relax the NN repulsion due to a kind of "anti-quark shielding" effect: uud-s \bar{u} -uud. The latter effect is not taken into account in our calculation, where the nucleons are treated as structureless elementary particles, but will certainly enhance the super strong nuclear force.

When the nuclear density exceeds the nucleon compaction factor, $2.3\rho_0$, an additional effect may come in, because the QCD vacuum is expected to vanish and chiral symmetry is restored.^{24)–26)} It is vitally important to investigate to what extent the involved hadrons keep their identities in such an extremely dense system.

7. The super strong nuclear force toward kaon condensation

We have studied many other kaonic bound states.⁸⁾ The strong bonding produced by a single \bar{K} was shown to saturate for 3-4 nucleons. We have also predicted the double- K^- clusters.⁹⁾ The species, K^-K^-pp , corresponds to the neutral hydrogen molecule, and has a large binding energy $B_{KK} = 117$ MeV and a shrunk inter-nucleon distance, $R_{N-N}^{\rm rms} = 1.3$ fm.⁹⁾ Expecting that the kaonic bound states with a large number of \bar{K} will be more deeply bound and stable, we proposed to search for them in high-energy heavy ion reactions.⁹⁾

We can conceive a multi- \overline{K} system, as sketched in Fig. 4 (Left), where K^- mesons migrate coherently among protons. We speculate that the ground state of such a system shows a large energy gap. The above consideration naturally leads us to a regime of kaon condensation.^{27), 28)} Namely, \bar{K} mesons, as intruders with \bar{u} and \bar{d} quarks, behave as strong glue to combine surrounding nucleons to a dense system. The whole energy drops down, depending on the composition of p, n and K. Intuitively, one can conceive energy diagrams as shown in Fig. 4 (Right). There are three phases: the \bar{K} matter with energy $E_K(\rho)$, the Λ matter with energy $E_{\Lambda}(\rho)$ and the normal nuclear matter with $E_N(\rho)$. Only the \bar{K} matter decreases in energy as the density increases. Then, there are three regimes for the phase stability.

i) $E_K(\rho) > E_\Lambda(\rho)$: strong decay to Λ 's [7.1] *ii*) $E_N(\rho) < E_K(\rho) < E_\Lambda(\rho)$:

weak decay :
$$\tau \sim$$
 sub-ns [7.2]

iii)
$$E_N(\rho) > E_K(\rho)$$
: stable [7.3]

Kaonic nuclear clusters in the cases i) and ii) can

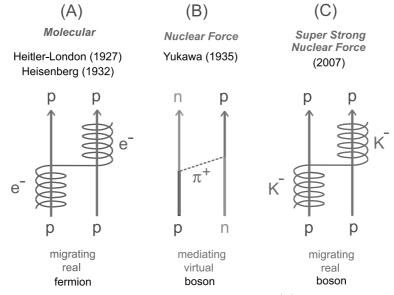


Fig. 5. Summary of the three different interaction schemes for nuclear forces. (A) The Heitler-London-Heisenberg model. (B) The Yukawa interaction. (C) The super strong nuclear force by the \bar{K} covalency.

be searched for in laboratory. The case iii) corresponds to a stable kaonic matter which might exist as a strange star.

In the present paper we have clarified that the \bar{K} meson can produce an enormously strong nucleonnucleon binding by the Heitler-London-Heisenberg mechanism. The \bar{K} -migrating NN bonding is deeper and longer-ranged with relatively smaller short-range repulsion. This super strong nuclear force can make ultra dense nuclear systems without the aid of gravity. Figure 5 summarizes the three kinds of nuclear forces, [1.1], [1.2] and [1.3].

Acknowledgements

We would like to thank Prof. P. Kienle for the stimulating discussion. One of us (T.Y.) is grateful to the Alexander von Humboldt Foundation for its "Forschungspreis". We acknowledge the receipt of Grant-in-Aid for Scientific Research of Monbu-Kagakusho of Japan.

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(Received April 23, 2007; accepted May 16, 2007)